

Chapter 8 Algebraic Expressions Ex 8.3

Question 1.

If $m = 2$, find the value of:

(i) $3m - 5$

(ii) $9 - 5m$

(iii) $3m^2 - 2m - 1$

(iv) $5m - 4$

Solution:

(i) $3m - 5 = 3 \times 2 - 5 = 6 - 5 = 1$

(ii) $9 - 5m = 9 - 5 \times 2 = 9 - 10 = -1$

(iii) $3m^2 - 2m - 1$

$= 3(2)^2 - 2 \times 2 - 1$

$= 12 - 4 - 1$

$= 12 - 5$

$= 7$

(iv) $\frac{5}{2}m - 4 = \frac{5}{2} \times 2 - 4 = 5 - 4 = 1$

Question 2.

If $p = -2$, find the value of:

(i) $4p + 7$

(ii) $-3p^2 + 4p + 7$

(iii) $-2p^3 - 3p^2 + 4p + 7$

Solution:

$$p = -2$$

$$(i) 4p + 7$$

$$= 4 \times (-2) + 7$$

$$= -8 + 7$$

$$= -1$$

$$(ii) -3p^2 + 4p + 7$$

$$= -3(-2)^2 + 4(-2) + 7$$

$$= -12 - 8 + 7$$

$$= -20 + 7$$

$$= -13$$

$$(iii) -2p^3 - 3p^2 + 4p + 7$$

$$= -2(-2)^3 - 3(-2)^2 + 4(-2) + 7$$

$$= 16 - 12 - 8 + 7$$

$$= 23 - 20$$

$$= 3$$

Question 3.

If $a = 2$, $b = -2$, find the value of:

(i) $a^2 + b^2$

(ii) $a^2 + ab + b^2$

(iii) $a^2 - b^2$

Solution:

$$a = 2, b = -2$$

$$(i) a^2 + b^2$$

$$= (2)^2 + (-2)^2$$

$$= 4 + 4$$

$$= 8$$

$$(ii) a^2 + ab + b^2$$

$$= (2)^2 + 2 \times (-2) + (-2)^2$$

$$= 4 - 4 + 4$$

$$= 8 - 4$$

$$= 4$$

$$(iii) a^2 - b^2$$

$$= (2)^2 - (-2)^2$$

$$= 4 - 4$$

$$= 0$$

Question 4.

When $a = 0$, $b = -1$, find the value of the given expressions:

(i) $2a^2 + b^2 + 1$

(ii) $a^2 + ab + 2$

(iii) $2a^2b + 2ab^2 + ab$

Solution:

$$a = 0, b = -1$$

$$(i) 2a^2 + b^2 + 1$$

$$= 2(0)^2 + (-1)^2 + 1$$

$$= 0 + 1 + 1$$

$$= 2$$

$$(ii) a^2 + ab + 2$$

$$= (0)^2 + 0 \times (-1) + 2$$

$$= 0 + 0 + 2$$

$$= 2$$

$$(iii) 2a^2b + 2ab^2 + ab$$

$$= 2(0)^2(-1) + 2(0)(-1)^2 + 0 \times (-1)$$

$$= 0 + 0 + 0$$

$$= 0$$

Question 5.

If $p = -10$, find the value of $p^2 - 2p - 100$.

Solution:

$$p = -10,$$

$$p^2 - 2p - 100$$

$$= (-10)^2 - 2(-10) - 100$$

$$= 100 + 20 - 100$$

$$= 20$$

Question 6.

If $z = 10$, find the value of $z^3 - 3(z - 10)$.

Solution:

$$z = 10$$

$$z^3 - 3(z - 10)$$

$$= (10)^3 - 3(10 - 10)$$

$$= 1000 - 3 \times 0$$

$$= 1000 - 0$$

$$= 1000$$

Question 7.

Simplify the following expressions and find their values when $x = 2$:

(i) $x + 7 + 4(x - 5)$

(ii) $3(x + 2) + 5x - 7$

(iii) $6x + 5(x - 2)$

(iv) $4(2x - 1) + 3x + 11$

Solution:

$$x = 2$$

$$(i) x + 7 + 4(x - 5)$$

$$= x + 7 + 4x - 20$$

$$= 5x - 13$$

$$= 5 \times 2 - 13$$

$$= 10 - 13$$

$$= -3$$

$$(ii) 3(x + 2) + 5x - 7$$

$$= 3x + 6 + 5x - 7$$

$$= 8x - 1$$

$$= 8(2) - 1$$

$$= 16 - 1$$

$$= 15$$

$$(iii) 6x + 5(x - 2)$$

$$= 6x + 5x - 10$$

$$= 11x - 10$$

$$= 11 \times 2 - 10$$

$$= 22 - 10$$

$$= 12$$

$$(iv) 4(2x - 1) + 3x + 11$$

$$= 8x - 4 + 3x + 11$$

$$= 11x + 7$$

$$= 11 \times 2 + 7$$

$$= 22 + 7$$

$$= 29$$

Question 8.

Simplify the following expressions and find their values when $a = -1$, $b = -2$:

(i) $2a - 2b - 4 - 5 + a$

(ii) $2(a^2 + ab) + 3 - ab$

Solution:

$$a = -1, b = -2$$

$$(i) 2a - 2b - 4 - 5 + a$$

$$= 3a - 2b - 9$$

$$= 3(-1) - 2(-2) - 9$$

$$= -3 + 4 - 9$$

$$= -12 + 4$$

$$= -8$$

$$(ii) 2(a^2 + ab) + 3 - ab$$

$$= 2a^2 + 2ab + 3 - ab$$

$$= 2a^2 + ab + 3$$

$$= 2(-1)^2 + (-1)(-2) + 3$$

$$= 2 \times 1 + 2 + 3$$

$$= 2 + 2 + 3$$

$$= 7$$