

Exercise 6

1. The sum of two numbers is 50 and their difference is 16. Find the numbers. Solution:

assume the two numbers to be x and y Then according to the given conditions, we have $x + y = 50 \dots$ (i)
and

$$x - y = 16 \dots \text{(ii)}$$

Now, adding (i) and (ii) we get $2x = 66$

$$x = 33$$

On substituting the value of x in (i), we get $33 + y = 50$

$$y = 50 - 33$$

$$y = 17$$

Therefore, the two numbers are 33 and 17.

2. The sum of two numbers is 2. If their difference is 20, find the numbers. Solution:

Let's assume the two numbers to be x and y Then according to the given conditions, we have $x + y = 2 \dots$
(i) and

$$x - y = 20 \dots \text{(ii)}$$

Now, adding (i) and (ii) we get $2x = 22$

$$x = 11$$

On substituting the value of x in (i), we get $11 + y = 2$

$$y = 2 - 11$$

$$y = -9$$

Therefore, the two numbers are 11 and -9.

3. The sum of two numbers is 43. If the larger is doubled and the smaller is tripled, the difference is 36. Find the two numbers.

Solution:

Let's assume the two numbers to be x and y such that $x > y$ Then according to the given conditions, we have

$$x + y = 43 \dots (i) \text{ and}$$

$$2x - 3y = 36 \dots (ii)$$

Now, multiplying (i) by 3 and adding with (ii) we get $3x + 3y = 129$

$$2x - 3y = 36$$

$$5x = 165$$

$$x = 165/5 = 33$$

On substituting the value of x in (i), we get $33 + y = 43$

$$y = 43 - 33$$

$$y = 10$$

Therefore, the two numbers are 33 and 10.

4. The cost of 5 kg of sugar and 7 kg of rice is Rs. 153, and the cost of 7 kg of sugar and 5 kg of rice is Rs. 147. Find the cost of 6 kg of sugar and 10 kg of rice.

Solution:

Let's assume the cost of 1 kg of sugar = Rs x

And, let the cost of 1 kg of rice = Rs y

Then according to the given conditions, we have

$$5x + 7y = 153 \dots (i) \text{ and}$$

$$7x + 5y = 147 \dots (ii)$$

Multiplying (i) by 7 and (ii) by 5, we have

$$35x + 49y = 1071 \dots (iii)$$

$$35x + 25y = 735 \dots (iv)$$

(-)-(-)-(-) Subtracting (iv) from (iii), we get

$$24y = 336 \quad y = 336/24 \quad y = 14$$

On substituting the value of y in (i), we get $5x + 7(14) = 153$

$$5x + 98 = 153$$

$$5x = 153 - 98$$

$$5x = 55$$

$$x = 55/5 = 11$$

So, the cost of 1 kg of sugar is Rs 11 and the cost of 1 kg of rice is Rs 14. Now,

Cost of 6 kg of sugar = Rs 11 x 6 = Rs 66 Cost of 10 kg of rice = Rs 14 x 10 = Rs 140

Thus, the cost of 6 kg of sugar and 10 kg of rice = Rs 66 + Rs 140 = Rs 206.

5. The class IX students of a certain public school wanted to give a farewell party to the outgoing students of class X. They decided to purchase two kinds of sweets, one costing Rs. 70 per kg and the other costing Rs. 84 per kg. They estimated that 36 kg of sweets were needed. If the total money spent on sweets was Rs. 2800, find how much sweets of each kind they purchased.

Solution:

Let the quantity of sweet costing Rs 70 be x And, the quantity of sweet costing Rs 84 be y

Given, total quantity of sweets purchased is 34 kg

$$x + y = 34 \dots (i)$$

Also given, the total money spent is Rs 2800

$$70x + 84y = 2800 \dots (ii)$$

Multiplying (i) by 70 and subtracting with (ii), we get $70x + 70y = 2520$

$$70x + 84y = 2800 \quad (-) \quad \text{---} \quad (-) \quad \text{-----} \quad (-) \quad \text{-----}$$

$$-14y = -280 \quad y = -280/-14 \quad y = 20$$

On substituting the value of y in equation (i), we get $x + 20 = 36$

$$x = 36 - 20$$

$$x = 16$$

Therefore, the quantities of sweets purchased are 16 kg which costs Rs 70 per kg and 20 kg which costs Rs 84 per kg.

6. If from twice the greater of two numbers 16 is subtracted, the result is half the other number. If from half the greater number 1 is subtracted, the result is still half the other number. What are the numbers.

Solution:

Let's consider the greater number to be x and the smaller number to be y .

Then, according to the given conditions we have $2x - 16 = y/2 \Rightarrow 4x - 32 = y \Rightarrow 4x - y = 32 \dots$ (i) And,

$x/2 - 1 = y/2 \Rightarrow x - 2 = y \Rightarrow x - y = 2 \dots$ (ii)

Now, subtracting (ii) from (i), therefore, the two numbers are 10 and 8.

7. There are 38 coins in a collection of 20 paise coins and 25 paise coins. If the total value of the collection is Rs. 8.50, how many of each are there?

Solution:

Subtracting (ii) from (i) we get $4x - y = 32$

$$x - y = 2$$

$$(-) - (+) = (-) \quad 3x = 30$$

$$x = 10$$

On substituting the value of x in (i), we get $2(10) - 16 = y/2$

$$20 - 16 = y/2$$

$$4 = y/2$$

$$y = 8$$

8. Let the number of 20 paise coins be x and let the number of 25 paise coins be y .

Then, according to the given conditions we have

$$x + y = 38 \dots$$
 (i) and

$$20x + 25y = 850 \dots$$
 (ii) [Since, 8.50 Rs = 850 paise] Performing (ii) - 20 x (i), we get

$$20x + 25y = 850$$

$$20x + 20y = 760 \quad (-) - (-) = (-) \quad \text{-----} \quad (-) \quad \text{-----}$$

$$5y = 90$$

$$y = 90/5 \quad y = 18$$

Substituting the value of y in (i), we have $x + 18 = 38$

$$x = 38 - 18$$

$$x/y = 2/3 \quad 3x = 2y$$

$$\Rightarrow 3x - 2y = 0 \dots (i)$$

Also given, if 2 is subtracted from the first and 8 from the second, the ratio becomes the reciprocal of the original ratio

$$(x - 2)/(y - 8) = 3/2$$

$$2(x - 2) = 3(y - 8)$$

$$2x - 4 = 3y - 24$$

$$\Rightarrow 2x - 3y = -20 \dots (ii)$$

Now, performing $3 \times (i) - 2 \times (ii)$ we get $9x - 6y = 0$

$$4x - 6y = -40$$

$$(-) - (+) - (-) - (+) - (-) - (-) \quad 5x = 40$$

$$x = 40/5 \quad x = 8$$

On substituting the value of x in (i), we get $3(8) - 2y = 0$

$$24 = 2y$$

$$y = 24/2 = 12$$

Therefore, the numbers are 8 and 12.

11. If 1 is added to the numerator of a fraction, it becomes $1/5$; if 1 is taken from the denominator, it becomes $1/7$, find the fraction.

Solution:

Let the fraction be x/y

Then according to the given conditions, we have $(x + 1)/y = 1/5$

$$5(x + 1) = y$$

$$5x + 5 = y$$

$$\Rightarrow 5x - y = -5 \dots (i)$$

And,

$$x/(y - 1) = 1/7 \quad 7x = y - 1$$

$$7x - y = -1 \dots (ii)$$

Now, subtracting (i) from (ii) we get $7x - y = -1$

$$5x - y = -5$$

$$(-)-(+)-(+)-\dots 2x = 4$$

$$x = 2$$

On substituting the value of x in (i), we get $5(2) - y = -5$

$$10 - y = -5$$

$$y = 10 + 5$$

$$y = 15$$

Therefore, the fraction is $2/15$.

12. If the numerator of a certain fraction is increased by 2 and the denominator by 1, the fraction becomes equal to $5/8$ and if the numerator and denominator are each diminished by 1, the fraction becomes equal to $1/2$, find the fraction.

Solution:

Let the fraction be x/y

Then according to the given conditions, we have $(x + 2)/(y + 1) = 5/8$

$$8(x + 2) = 5(y + 1)$$

$$8x + 16 = 5y + 5$$

$$8x - 5y = 5 - 16$$

$$8x - 5y = -11 \dots (i)$$

And,

$$(x - 1)/(y - 1) = 1/2$$

$$2(x - 1) = (y - 1)$$

$$2x - 2 = y - 1$$

$$2x - y = 1 \dots (ii)$$

Now, performing (i) $- 4 \times$ (ii) we get $8x - 5y = -11$

$$8x - 4y = 4 \quad (-) - (+) - (-)$$

$$-y = -15$$

$$y = 15$$

On substituting the value of y in (ii), we get $2x - 15 = 1$

$$2x = 1 + 15 \quad x = 16/2 = 8$$

Therefore, the fraction is $8/15$.

13. Find the fraction which becomes $\frac{1}{2}$ when the denominator is increased by 4 and is equal to $\frac{1}{8}$, when the numerator is diminished by 5.

Solution:

Let the fraction be x/y .

Then according to the given conditions, we have $x/(y + 4) = \frac{1}{2}$

$$2x = y + 4$$

$$2x - y = 4 \dots (i)$$

And,

$$(x - 5)/y = 1/8 \quad 8(x - 5) = y$$

$$8x - 40 = y$$

$$8x - y = 40 \dots (ii)$$

Now, subtracting (i) from (ii) we get $8x - y = 40$

$$2x - y = 4$$

$$(-) - (+) - (-) - (-) \dots 6x = 36$$

$$x = 36/6 \quad x = 6$$

On substituting the value of x in (i), we get $2(6) - y = 4$

$$12 - y = 4$$

$$y = 12 - 4 = 8$$

Therefore, the fraction is $6/8$.

14. In a two-digit number the sum of the digits is 7. If the number with the order of the digits reversed is 28 greater than twice the unit's digit of the original number, find the number. Solution:

Let's consider the digit at tens place as x

And let the digit at unit place be y

Then according to the first condition, we have $x + y = 7$... (i)

Also, the number = $10 \times x + y \times 1 = 10y + x$ Now, according to the second condition we have $10y + x = 2y + 28$

$$x + 8y = 28 \dots (ii)$$

Subtracting (i) from (ii), we get $x + 8y = 28$

$$x + y = 7$$

$$(-) - (-) - (-) \quad 7y = 21$$

$$y = 21/7 \quad y = 3$$

Substituting the value of y in (i), we get $x + 3 = 7$

$$x = 7 - 3$$

$$x = 4$$

Therefore, the number is $10 \times 4 + 3 = 43$.

15. A number of two digits exceeds four times the sum of its digits by 6 and it is increased by 9 on reversing the digits. Find the number.

Solution:

Let's consider the digit at tens place as x

And let the digit at unit place be y

The number is $10 \times x + y \times 1 = 10x + y$

So, reversing the number = $10 \times y + x \times 1 = 10y + x$ Then according to the first condition, we have

$$10x + y = 4(x + y) + 6$$

$$10x - 4x + y - 4y = 6 \quad 6x - 3y = 6$$

$$2x - y = 2 \dots (i)$$

And according to the second condition, we have $10x + y + 9 = 10y + x$

$$10x - x + y - 10y = -9$$

$$9x - 9y = -9$$

$$x - y = -1 \dots (ii)$$

Now, subtracting (ii) from (i) we have $2x - y = 2$

$$x - y = -1$$

$$(-) - (+) - (-) = -$$

$$x = 3$$

Substituting the value of x in (i), we get $2(3) - y = 2$

$$6 - y = 2$$

$$y = 6 - 2$$

$$y = 4$$

Therefore, the number is $10 \times 3 + 4 = 30 + 4 = 34$.

16. When a two-digit number is divided by the sum of its digits the quotient is 8. If the ten's digit is diminished by three times the unit's digit the remainder is 1. What is the number?

Solution:

Let's consider the digit at tens place as x

And let the digit at unit place be y

The number is $10 \times x + y \times 1 = 10x + y$

Then according to the first condition, we have $(10x + y) / (x + y) = 8$

$$10x + y = 8(x + y) \quad 10x + y = 8x + 8y \quad 10x - 8x + y - 8y = 0 \quad 2x - 7y = 0 \dots (i)$$

And according to the second condition, we have $x - 3y = 1 \dots (ii)$

Performing (i) - 2 x (ii), we get $2x - 7y = 0$

$$2x - 6y = 2 \quad (-) - (+) - (-)$$

$$-y = -2$$

$$y = 2$$

Substituting the value of y in (i), we get

$$2x - 7(2) = 0$$

$$2x = 14$$

$$x = 14/2 \quad x = 7$$

Therefore, the number is $= 10 \times 7 + 2 = 70 + 2 = 72$.

17. The result of dividing a number of two digits by the number with digits reversed is $1\frac{3}{4}$. If the sum of digits is 12, find the number.

Solution:

Let's consider the digit at tens place as x

And let the digit at unit place be y

The number is $10 \times x + y \times 1 = 10x + y$

So, reversing the number $= 10 \times y + x \times 1 = 10y + x$

Then according to the first condition given in the problem, we have $(10x + y) / (10y + x) = 1\frac{3}{4}$

$$(10x + y) / (10y + x) = 7/4 \quad 4(10x + y) = 7(10y + x)$$

$$40x + 4y = 70y + 7x \quad 40x - 7x - 70y + 4y = 0$$

$$33x - 66y = 0$$

$$x - 2y = 0 \quad \dots \text{ (i)}$$

And according to the second condition of the given problem, we have

$$x + y = 12 \quad \dots \text{ (ii)}$$

From equation (i) and (ii), we have $x + y = 12$

$$x - 2y = 0$$

$$(-) - (+) - (-) \quad 3y = 12$$

$$y = 12/3 \quad y = 4$$

On substituting the value of y in (i), we have $x - 2(4) = 0$

$$x = 8$$

Therefore, the number is $10 \times 8 + 4 = 84$.

18. The result of dividing a number of two digits by the number with the digits reversed is $\frac{5}{6}$. If the difference of digits is 1, find the number.

Solution:

Let's consider the digit at tens place as x

And let the digit at unit place be y

The number is $10 \times x + y \times 1 = 10x + y$

So, reversing the number = $10 \times y + x \times 1 = 10y + x$

Then according to the first condition given in the problem, we have $(10x + y) / (10y + x) = \frac{5}{6}$

$$6(10x + y) = 5(10y + x)$$

$$60x + 6y = 50y + 5x \quad 60x - 5x - 50y + 6y = 0$$

$$55x - 44y = 0$$

$$5x - 4y = 0 \dots (i) \text{ [Dividing by 11 on both sides]}$$

And, according to the second condition in the given problem, we have $y - x = 1$

$$-x + y = 1 \dots (ii)$$

Performing (i) + 5 x (ii), we get $5x - 4y = 0$

$$-5x + 5y = 5$$

$$y = 5$$

On substituting the value of y in equation (i), we have $5x - 4(5) = 0$

$$5x - 20 = 0$$

$$5x = 20$$

$$x = \frac{20}{5} \quad x = 4$$

Therefore, the number is $10 \times 4 + 5 = 40 + 5 = 45$.

19. A number of three digits has the hundred digit 4 times the unit digit and the sum of three digits is 14. If the three digits are written in the reverse order, the value of the number is decreased by 594. Find the number.

Solution:

Let's consider the digit at tens place as x

And let the digit at unit place be y Then, the digit at hundred place = $4y$

Hence, the number is $100 \times 4y + 10 \times x + y \times 1 = 400y + 10x + y = 401y + 10x$

So, reversing the number = $100 \times y + 10 \times x + 4y \times 1 = 100y + 10x + 4y = 104y + 10x$ Then according to the first condition given in the problem, we have

$$x + y + 4y = 14$$

$$x + 5y = 14 \dots (i)$$

And according to the second condition given in the problem, we have $401y + 10x = 104y + 10x + 594$

$$401y - 104y = 594$$

$$297y = 594 \quad y = 594/297$$

$$y = 2$$

On substituting the value of y in equation (i), we have $x + 5(2) = 14$

$$x + 10 = 14$$

$$x = 14 - 10$$

$$x = 4$$

Therefore, the number is = $10x + 401y = 10(4) + 401(2) = 40 + 802 = 842$.

20. Four years ago Marina was three times old as her daughter. Six years from now the mother will be twice as old as her daughter. Find their present ages.

Solution:

Let take the present age of Marina as x years and The present age of Marina's daughter as y years. Now, four years ago

Age of Marina will be $(x - 4)$ years

Age of Marina's daughter will be $(y - 4)$ years

According to the first condition given in the problem, we have $(x - 4) = 3(y - 4)$

$$x - 4 = 3y - 12$$

$$x - 3y = -8 \dots (i)$$

Now, the age of Maria after 6 years will be $(x + 6)$ years

And the age of Maria's daughter will be $(y + 6)$ years

Then, according to the second condition given in the problem, we have $x + 6 = 2(y + 6)$

$$x + 6 = 2y + 12$$

$$x - 2y = 6 \dots \text{(ii)}$$

From equations (i) and (ii), we get $x - 2y = 6$

$$x - 3y = -8 \quad (-) \quad (-) \quad (+) \quad (-) \quad (+) \quad y = 14$$

On substituting the value of y in (i), we get $x - 3 \times 14 = -8$

$$x - 42 = -8$$

$$x = -8 + 42$$

$$x = 34$$

Therefore, the age of Marina is 34 years and the age of her daughter is 14 years.

21. On selling a tea set at 5% loss and a lemon set at 15% gain, a shopkeeper gains Rs. 70. If he sells the tea set at 5% gain and lemon set at 10% gain, he gains Rs. 130. Find the cost price of the lemon set.

Solution:

Given,

Loss on tea set = 5% and Gain on lemon set = 15%

Let's assume the C.P of tea set = Rs x and

The C.P of lemon set = Rs y

Then according to the given conditions, we have

$$15y - 5x = 7000$$

$$-x + 3y = 1400 \dots \text{(i)}$$

And,

$$5x + 10y = 13000$$

$$x + 2y = 2600 \dots (ii)$$

Now, adding (i) and (ii) we get

$$-x + 3y = 1400 \quad x + 2y = 2600$$

$$\text{-----} \quad 5y = 4000$$

$$y = 4000/5 \quad y = 800$$

Therefore, the Cost price of lemon set = Rs 800.

22. A person invested some money at 12% simple interest and some other amount at 10% simple interest. He received yearly interest of Rs, 1300. If he had interchanged the amounts, he would have received Rs. 40 more as yearly interest. How much did he invest at different rates? Solution:

Let the amount invested at S.I be Rs x at rate = 12% p.a. And another investment at S.I = Rs y at rate = 10% p.a. Then according to the given conditions, we have

$$12x + 10y = 130000$$

$$6x + 5y = 65000 \dots (i)$$

And,

$$10x + 12y = 134000$$

$$5x + 6y = 67000 \dots (ii)$$

Multiplying (i) by 6 and (ii) by 5, we have $36x + 30y = 390000$

$$25x + 30y = 335000 \quad (-) \quad (-) \quad \text{-----} \quad (-) \quad \text{-----}$$

$$11x = 55000 \quad x = 55000/11 \quad x = 5000$$

On substituting the value of x in (i), we get $6(5000) + 5y = 65000$

$$30000 + 5y = 65000$$

$$5y = 65000 - 30000 \quad y = 35000/5 = 7000$$

Therefore, the investment at 12% is Rs 5000 and the investment at 10% is Rs 7000.

23. A shopkeeper sells a table at 8% profit and a chair at 10% discount, thereby getting Rs.1008. If he had sold the table at 10% profit and chair at 8% discount, he would have got Rs. 20 more. Find the cost price of the table and the list price of the chair.

Solution:

Given,

Profit on table = 8% Discount on chair = 10%

Let C.P. of table = Rs x and C.P. of chair = Rs y Then according to the given condition, we have

$$108x + 90y = 100800$$

$$6x + 5y = 5600 \dots(i)$$

And,

$$110x + 92y = 102800$$

$$55x + 46y = 51400 \dots(ii)$$

Now, multiplying (i) by 55 and (ii) by 6, we have $330x + 275y = 308000$

$$330x + 276y = 308400 \quad (-) \quad \text{-----} \quad (-) \quad \text{-----}$$

$$-y = -400$$

$$y = 400$$

On substituting the value of y in equation (i), we get $6x + 5(400) = 5600$

$$6x = 5600 - 2000 \quad x = 3600/6$$

$$x = 600$$

Therefore, the C.P. of table = Rs 600 and the C.P. of chair = Rs 400.

24. A and B have some money with them. A said to B, "if you give me Rs. 100, my money will become 75% of the money left with you." B said to A " instead if you give me Rs. 100, your money will become 40% of my money. How much money did A and B have originally?

Solution:

Let's assume A has money = x

$$-2x + y = 2 \dots (i)$$

And, according to the second condition given in the problem, we have $(x - 1)(y + 3) = xy$

$$xy + 3x - y - 3 = xy \quad 3x - y = 3 \dots (ii)$$

Adding equations (i) and (ii), we get

$$-2x + y = 2$$

$$3x - y = 3$$

$$x = 5$$

On substituting the value of x in equation (i), we have

$$-2(5) + y = 2$$

$$-10 + y = 2$$

$$y = 2 + 10$$

$$y = 12$$

Therefore, the number of students = $xy = 5 \times 12 = 60$.

26. A jeweler has bars of 18-carat gold and 12-carat gold. How much of each must be melted together to obtain a bar of 16-carat gold weighing 120 grams? (Pure gold is 24 carat)

Solution:

Let's assume the quantity of 18 carat gold as x gm and 12 carat gold as y gm.

Then according to the first condition given in the problem, we have

$$x + y = 120 \dots (i)$$

Pure gold is 24 carat

So, the purity of 18 carat gold = $(18/24) \times 100\%$

$$= \left(\frac{3}{4}\right) \times 100$$

$$= 75\%$$

Purity of 12 carat gold = $(12/24) \times 100\%$

$$= \frac{1}{2} \times 100\%$$

$$= 50\%$$

And, the purity of 16 carat gold = $(16/24) \times 100\%$

$$= (2/3) \times 100\%$$

$$= 200/3\%$$

Now, according to the second condition given in the problem, we have $75x + 50y = 200/3 \times 120$

$$75x + 50y = 200 \times 40$$

$$75x + 50y = 8000$$

$3x + 2y = 320$... (ii) Performing (ii) $- 2 \times$ (i), we get $3x + 2y = 320$

$$2x + 2y = 240 \text{ --- (-)--- (-)--- (-)--- } x = 80$$

On substituting the value of x in equation (i), we get $80 + y = 120$

$$y = 120 - 80$$

$$y = 40$$

Therefore, the jeweler requires 80 gm of 18 carat gold and 40 gm of 12 carat gold to obtain a bar of 16 carat gold weighing 120 gm.

27. A and B together can do a piece of work in 15 days. If A's one day work is $1\frac{1}{2}$ times the one day's work of B, find in how many days can each do the work.

Solution:

Let A's one day work be x and B's one day work be y.

Then according to the first condition given in the problem, we have $x = (3/2)y$

$$2x = 3y$$

$$2x - 3y = 0 \text{ ... (i)}$$

Also given, in 15 days: A and B together can do a piece of work

So, according to this condition we have $x + y = 1/15$

$$15(x + y) = 1$$

$$15x + 15y = 1 \text{ ... (ii)}$$

Multiplying equation (i) by 5, we get $10x - 15y = 0$

$$15x + 15y = 1$$

$$\text{----- } 25x = 1$$

$$x = 1/25$$

On substituting the value of x in equation (i), we get $2(1/25) - 3y = 0$

$$2/25 = 3y$$

$$y = 2/75$$

Therefore, Man A will do the work in $1/x$ days = $1/(1/25) = 25$ day and Man B will do the work in $(1/y)$ days = $1/(2/75) = 75/2 = 37\frac{1}{2}$ days.

28.2 men and 5 women can do a piece of work in 4 days, while one man and one woman can finish it in 12 days. How long would it take for 1 man to do the work?

Solution:

Let's assume that 1 man takes x days to do work and y days for a woman. So, the amount of work done by 1 man in 1 day = $1/x$

And the amount of work done by 1 woman in 1 day = $1/y$ Now,

The amount of work done by 2 men in 1 day will be = $2/x$ And the amount of work done by 5 women in 1 day = $5/y$

Then according to the given conditions in the problem, we have $2/x + 5/y = \frac{1}{4}$... (i)

$$1/x + 1/y = 1/12 \text{ ... (ii)}$$

Multiplying equation (ii) by 5, we get $5/x + 5/y = 5/12$

$$2/x + 5/y = \frac{1}{4} \text{ --- (-) --- (-) --- (-)}$$

$$3/x = 5/12 - \frac{1}{4}$$

$$3/x = (5 - 3)/12$$

$$3/x = 2/12 = 1/6 \quad x = 18$$

Therefore, 1 man can do the work in 18 days.

29. A train covered a certain distance at a uniform speed. If the train had been 30 km/hr faster, it would have taken 2 hours less than the scheduled time. If the train were slower by 15 km/hr, it would have taken 2 hours more than the scheduled time. Find the length of the journey.

Solution:

Let the actual speed of the train be x km/hr and the scheduled time be y hours.

Then, the distance of the journey = speed x time = xy According to the given conditions in the problem, we have $(x + 30)(y - 2) = xy$

$$xy - 2x + 30y - 60 = xy$$

$$-2x + 30y = 60 \dots (i)$$

And,

$$(x - 15)(y + 2) = xy$$

$$xy - 15y + 2x - 30 = xy \quad 2x - 15y = 30 \dots (ii)$$

From equations (i) and (ii), we have

$$-2x + 30y = 60 \quad 2x - 15y = 30$$

$$\text{-----} \quad 15y = 90$$

$$y = 90/15$$

$$y = 6$$

On substituting the value of y in (i), we have

$$-2x + 30(6) = 60$$

$$-2x + 180 = 60$$

$$-2x = 60 - 180 = -120 \quad x = -120/-2$$

$$x = 60$$

Therefore, the distance of the journey = $60 \times 6 = 360$ km.

30. A boat takes 2 hours to go 40 km down the stream and it returns in 4 hours. Find the speed of the boat in still water and the speed of the stream.

Solution:

Let's assume the speed of the boat in still water be x km/hr

And the speed of the stream = y km/hr

So, the speed of the boat in downstream = $(x + y)$ km/hr The speed of the boat in upstream = $(x - y)$ km/hr

We know,

Distance = Speed x time

Now, according to the given conditions in the problem, we have $40 = (x + y) \times 2$

$$x + y = 20 \dots (i)$$

And,

$$40 = (x - y) \times 4$$

$$x - y = 10 \dots (ii)$$

Adding (i) and (ii), we have $x + y = 20$

$$x - y = 10$$

$$\text{-----} \quad 2x = 30$$

$$x = 15$$

On substituting the value of x in equation (i), we have $15 + y = 20$

$$y = 20 - 15$$

$$y = 5$$

Therefore, speed of the boat in still water = 15 km/hr and speed of the stream = 5 km/hr.

31. A boat sails a distance of 44 km in 4 hours with the current. It takes 4 hours 48 minutes longer to cover the same distance against the current. Find the speed of the boat in still water and the speed of the current.

Solution:

Let's assume the speed of the boat in still to be x km/hr

And the speed of the current = y km/hr

Speed of the boat in the direction of current = $(x + y)$ km/hr
Speed of the boat against the current = $(x - y)$ km/hr

We know, distance = speed \times time

Then according to the given conditions in the problem, we have $44 = (x + y) \times 4$

$$x + y = 44/4$$

$$x + y = 11 \dots (i) \text{ And,}$$

$$x - y = 5 \dots (ii)$$

Now, adding equations (i) and (ii) we have $x + y = 11$

$$x - y = 5$$

$$\text{----- } 2x = 16$$

$$x = 16/2 \quad x = 8$$

On substituting the value of x in (i), we get $8 + y = 11$

$$y = 11 - 8$$

$$y = 3$$

Therefore, the speed of the boat in still water = 8 km/hr and speed of the current = 3 km/hr.

32. An aeroplane flies 1680 km with a head wind in 3.5 hours. On the return trip with same wind blowing, the plane takes 3 hours. Find the plane's air speed and the wind speed.

Solution:

Let's assume the speed of the plane = x km/hr

And let the speed of wind = y km/hr

So, the speed of the aeroplane in the direction of wind = $(x + y)$ km/hr
Speed of the aeroplane in the opposite direction of wind = $(x - y)$ km/hr
We know, distance = speed \times time

Then according to the given conditions, we have $1680 = (x - y) \times 3.5$

$$x - y = 1680/3.5$$

$$x - y = 480 \dots (i)$$

And,

$$1680 = (x + y) \times 3 \quad x + y = 1680/3$$

$$x + y = 560 \dots (ii)$$

From equation (i) and (ii), we get $x - y = 480$

$$x + y = 560$$

$$\text{----- } 2x = 1040$$

$$x = 1040/2 = 520$$

Substituting the value of x in equation (i), we get $520 - y = 480$

$$y = 520 - 480$$

$$y = 40$$

Therefore, the speed of aeroplane = 520 km/hr and the speed of wind = 40 km/hr.

33. A part of monthly hostel charges is fixed and the remaining depends on the number of days one has taken food in the mess. When Bhawana takes food for 20 days, she has to pay Rs. 2600 as hostel charges; whereas when Divya takes food for 26 days, she pays Rs. 3020 as hostel charges. Find the fixed charges and the cost of food per day.

Solution:

Let the fixed charges = Rs x and The charges per day = Rs y

Then according to the given conditions, we have

$$x + 20y = 2600 \dots (i)$$

$$x + 26y = 3020 \dots (ii)$$

(-)-(-)-(-) On subtracting, we get

$$-6y = -420 \quad y = 420/6 \quad y = 70$$

Substituting the value of y in (i), we get $x + 20 \times 70 = 2600$

$$x = 2600 - 1400$$

$$x = 1200$$

Therefore, the fixed charges = Rs 1200 and daily charges = Rs 70.